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# Mathematics in our research work



Mathematics in our research work 2

9 December 2021 DTU Chemical Engineering



### PROSYS

- Process Systems Engineering (PSE)
- Process Intensification and Integration (PII)
- Process design and control
- Industrial fermentation technology
- Biocatalysis
- Microfluidics

### Very practically, we work with ...

- Computational Fluid Dynamics
- Novel sensor equipment
- Digital twins and process simulation
- Scale-up / scale-down
- Novel processes
- Artificial intelligence / machine learning
- Process design / process optimisation



### Introduction

### Putting things in perspective ...

#### The use of a model



### **Applied mathematics!**

# DTU **Digital twin**

#### The buzzwords:

- Big data?
- AI Machine learning
- Industry 4.0



The ability to collect and process sufficient data is essential!!



Udugama et al. (2020) Industrial & Engineering Chemistry Research, 59, 15283-15297.





pubs.acs.org/IECR

Article

#### The Role of Big Data in Industrial (Bio)chemical Process Operations

Isuru A. Udugama, Carina L. Gargalo, Yoshiyuki Yamashita, Michael A. Taube, Ahmet Palazoglu, Brent R. Young, Krist V. Gernaey, Murat Kulahci, and Christoph Bayer\*



**ABSTRACT:** With the emergence of Industry 4.0 and Big Data initiatives, there is a renewed interest in leveraging the vast amounts of data collected in (bio)chemical processes to improve their operations. The objective of this article is to provide a perspective of the current status of Big-Data-based process control methodologies and the most effective path to further embed these methodologies in the control of (bio)chemical processes. Therefore, this article provides an overview of operational requirements, the availability and the nature of data, and the role of the control structure hierarchy in (bio)chemical processes and how they constrain this endeavor. The current state of the seemingly competing methodologies of statistical process monitoring and (engineering) process control is examined together with hybrid methodologies that are attempting to combine tools and techniques.





# Systems of coupled differential equations

# Essential in an environment driven by first principles models ...

#### **Kinetic equations**

• Growth (Monod equation)

$$r_X = \mu C_X = \left(\frac{\mu_{max}C_S}{K_S + C_S}\right) C_X[kg \ m^{-3} \ h^{-1}]$$
Biomass formation rate

• Substrate uptake (Herbert-Pirt equation)

$$r_S = q_S C_X = \left(\frac{\mu}{Y_{XS}} + m_S\right) C_X [kg \ m^{-3} \ h^{-1}]$$
 Substrate uptake rate

Product formation (Luedeking-Piret equation)

$$r_P = q_P C_X = \left(\frac{\mu}{Y_{XP}} + \beta\right) C_X [kg \ m^{-3} \ h^{-1}]$$
 Product formation rate

 $C_X$  = biomass concentration;  $C_S$  = substrate concentration;  $K_S$  = half-saturation constant;  $\mu$  = specific growth rate;  $\mu_{max}$  = maximum specific growth rate;  $Y_{XS}$  = Yield coefficient, mass of biomass formed per mass of substrate consumed  $Y_{XP}$  = Yield coefficient, mass or biomass formed per mass of product produced;  $q_S$  = specific substrate uptake rate;  $q_P$  = specific product formation rate;  $m_S$  = maintenance coefficient;  $\alpha$ ,  $\beta$  = coefficients;

#### **Types of bioreactor operation**









# Application example: Modelling of a full-scale industrial granular anaerobic digester

Xavier Flores-Alsina, Hannah Feldman, Pedram Ramin, Krist V. Gernaey: PROSYS, DTU, Denmark Kasper Kjellberg: Novozymes, Denmark Damien Batstone: AWMC, University of Queensland, Australia Ulf Jeppsson: IEA, Lund University, Sweden



- Industrial wastewater
- Q = 150 m<sup>3</sup>.h<sup>-1</sup>
- COD = 1600 kg COD.h<sup>-1</sup>
- $N = 70 \text{ kg.h}^{-1}$
- P = 40 kg.h<sup>-1</sup>
- S:COD = 0.025 kg/kg

#### **Multi-scale modelling representation**



Feldman et al. (2018) Biotechnology & Bioengineering, 115, 2726-2739.



#### Model testing: Data set #1

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### Ongoing work





Novozymes and Novo Nordisk production site Kalundborg, Denmark

### **Ongoing work – increased complexity!**



Monje et al. (2021) Journal of Environmental Management, 293, 112806.



# Optimization

# When the best process is the only thing that is good enough ...

### **Glycerol Biorefinery – superstructure optimization**



**Mathematical optimization** (e.g. superstructure optimization) is used to identify the best candidates, under process, business and environmental constraints – on the path to sustainable designs

is very promising

### **Bio-chemicals from glycerol fermentation**



#### Another example - Beer fermentation model

included in the model (system of differential equations):

- $\checkmark$  sugar and amino acids uptake
- ✓ yeast growth
- ✓ ethanol production
- ✓ formation of four fusel alcohols (isobutanol, isoamyl alcohol, 2-methyl-1-butanol and n-propanol)
- ✓ formation of three esters (ethyl acetate, ethyl hexanoate and isoamyl acetate)
- ✓ VDKs and

D

✓ acetaldehyde.



#### Optimization strategy

- The goal is to obtain an optimal temperature and flavor profile
- Sequential Quadratic Programming (SQP), Sequential Annealing (SA) and Genetic Algorithm (GA) were considered as optimization strategies
- Genetic algorithm was selected as the optimization strategy → avoids local minima and it provides a better exploration of the search space



#### To minimize

Concentrations of off-flavors: fusel alcohols, VDKs and acetaldehyde

#### Fermentation time

#### To maximize

Concentrations of on- flavors: ethanol and esters

Thresholds of detection + max/min concentrations are respected → acting as model constraints

#### To penalize

- large fermentation times
- low concentrations of on-flavors
- high concentrations of off-flavors



#### Optimization scenarios

# FF(O4) $FF(O_1) = Q_{IB} + Q_{IA} + Q_{MB} + Q_P + Q_{EA} + Q_{EC} + Q_{IAc} + Q_{VDK} + Q_{AAI} + Q_{EtOH} + Q_t$ FF(O3)

O1 ('master') = All the variables are included

O2 = Time and ethanol

O3 = Time and maximization variables

O4 = Time and minimization variables

Fitness function definition (500 individuals population)

$$Q_i = \frac{\left([i]_f - [i]_{min}\right)^2}{i_{desv}^2} \qquad FF = \sum Q_i$$

 $i = variables to optimize \rightarrow [species] and time$ 

#### Results

					287.5	
	<b>O</b> <sub>1</sub>	<b>O</b> <sub>2</sub>	<b>O</b> <sub>3</sub>	<b>O</b> <sub>4</sub>	287 -	
FF	2.3970	0.0260	0.4640	1.5563	207	
Qalcohols	0.7855	7.6201	5.8161	0.0000	€ 286.5	
Q <sub>esters</sub>	0.4803	1.5946	0.3369	30.3103	- 286 -	
Q <sub>AAI</sub>	0.1349	0.1947	0.1768	0.0000	285.5 -	-
Q <sub>VDK</sub>	0.0087	0.0000	0.0000	1.5538	285 -	
Q <sub>EtOH</sub>	0.0855	0.0235	0.0045	4.0986	004.5	
Q <sub>t</sub>	0.9025	0.0025	0.1225	0.0025	284.0	
t <sub>F</sub>	140.0	121.7	127.3	122.0	284 -	







# **Applied statistics**

# Random phenomena are inherently present in any process we study ...

### **Uncertainty and sensitivity analysis**

- Sensitivity analysis "studies how variation (uncertainty) in the outputs of a model can be apportioned to different sources in the input of a model"
- SA complimentary to uncertainty analysis: "quantifying uncertainty in the outputs of a model from uncertainty in its inputs"



#### **Uncertainty and sensitivity analysis**



Gernaey et al. (2010) Trends Biotechnol., 28:346-354.

### Example: Ethanol Fermentation Model – data generator



Comp. → Process $\downarrow$	X <sub>bio</sub>	Glu	Xyl	Eth	Fur	Ac	HMF	FA	TIC
Glu uptake	Y <sub>X/Glu</sub>	-1	0	Y <sub>Eth/Glu</sub>	0	0	0	0	Y <sub>CO2/Glu</sub>
Xyl uptake	Y <sub>X/Xyl</sub>	0	-1	Y <sub>Eth/Xyl</sub>	0	0	0	0	Y <sub>CO2/Xyl</sub>
Fur uptake	~ 0	0	0	0	-1	0	0	Y <sub>FA/Fur</sub>	0
Ac uptake	~ 0	0	0	0	0	-1	0	0	Y <sub>CO2/Ac</sub>
HMF uptake	~ 0	0	0	0	0	Y <sub>Ac/HMF</sub>	-1	0	0
	Equat	ion ex	press	sed as sub	strate	consumpt	tion		
Glu uptake	$v_{Max}X_{l}$	rio K <sub>SGh</sub>	Glu $_i+Glu+$	$\frac{\frac{Gl u^2}{K_{IGlu}}}{\frac{1}{1 + \frac{Fu}{J_{Fu}}}}$	$\frac{r}{r}$ $\frac{1}{1+\frac{H}{J_I}}$	$\frac{1}{\frac{MF}{IMF}} \frac{1}{1 + \frac{HAc}{J_{HAc}}}$	I(Xyl, I	Eth, pH)	
Xyl uptake	$v_{Max}X_{l}$	nio K <sub>SXy</sub>	Xyl l+Xyl+	$\frac{Xyl^2}{K_{IXyl}} \frac{1}{1 + \frac{Fw}{J_{Fb}}}$	$\frac{r}{r}$ $\frac{1}{1+\frac{H}{J_I}}$	$\frac{1}{\frac{MF}{IMF}} \frac{1}{1 + \frac{HAc}{J_{HAc}}}$	I(Glu, H	Eth, pH)	
Fur uptake	$v_{Max}X_{l}$	nio $\frac{F}{K_{SFu}}$	ur +Fur						
Ac uptake	$v_{Max}X_{l}$	nio $\frac{A}{K_{SAc}}$	$\frac{c}{+Ac}$						
HMF uptake	$v_{Max}X_{l}$	no $\frac{F}{K_{SFw}}$	$\frac{ur}{r+Fur}$						



### Ethanol Big Data Generator $\rightarrow$ Teaching



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### **Conclusions / future perspectives**

- Mathematical modelling as a versatile tool to support our daily work focus on applications!
- Increased computing power leads to larger systems to be solved basic methods the same
- Matlab, Python, ANSYS CFX as most frequently used software tools
- In recent years: increasing focus on combination of first principles and data-driven approaches hybrid models
- Dare to share!!!



#### **Contact details**

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